## Low-frequency shallow water reverberation and bottom scattering model

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#### Introduction

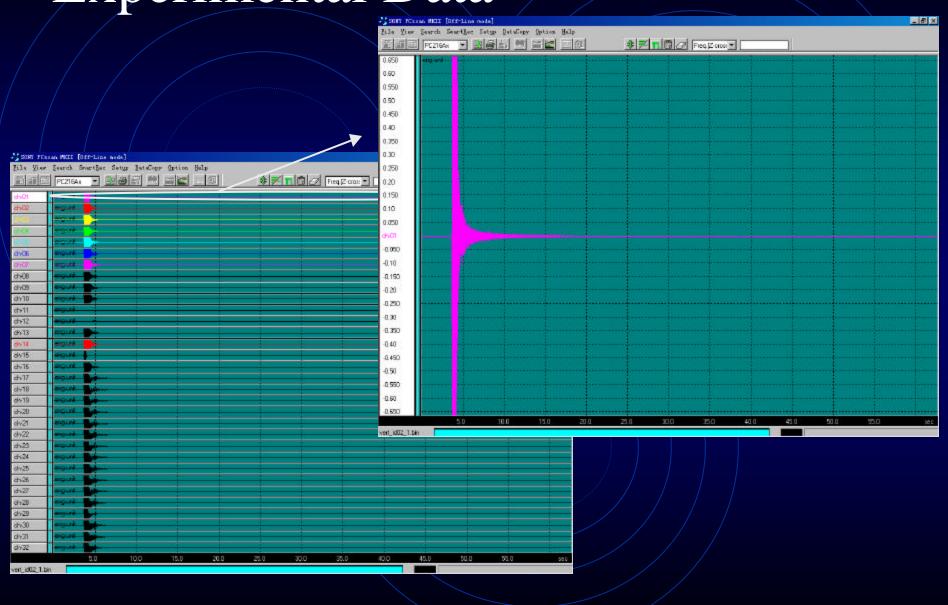
- The problems of reverberation model
  - Propagation model
  - Bottom parameters
  - Scattering model
    - Angle relationship
    - Frequency relationship
    - Physical mechanism
- Motivation of this talk
  - The ASIAEX01 reverberation data are used to validate different bottom scattering models.

#### Contents

- Middle frequency (700Hz to 2000Hz, in this report) reverberation loss to validate different bottom scattering models.
- Low frequency (<700Hz) reverberation loss and sediment-basement combined scattering model.

# 1. Middle Frequency reverberation data

## Experimental Data



#### Data analysis procession

Recorded data x(t)

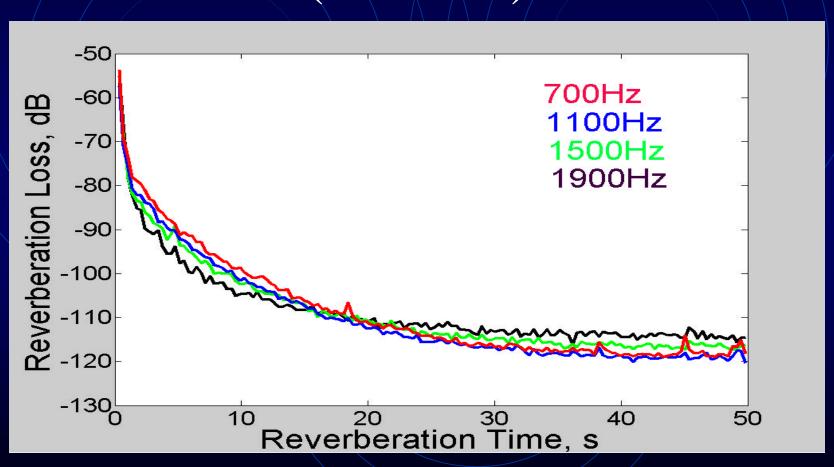
Narrow band filtering y(t)=filter(x(t))

Short time energy average I(t0)=mean( $y^2(t)$ )

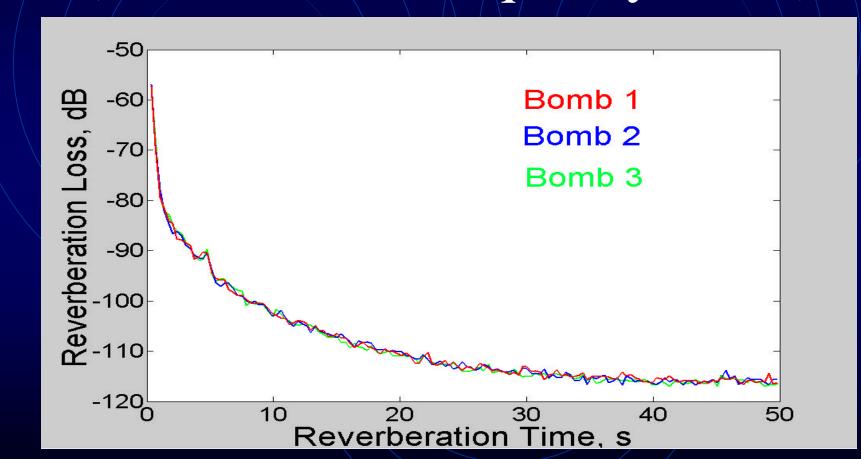
(t=t0 to t0+dt)

Reverberation loss RL(t)=10\*log10(I(t))-SL

## Reverberation loss vs. time (Bomb 1)



# Reverberation loss vs. time (Bomb 1/2/3, Frequency 1kHz)



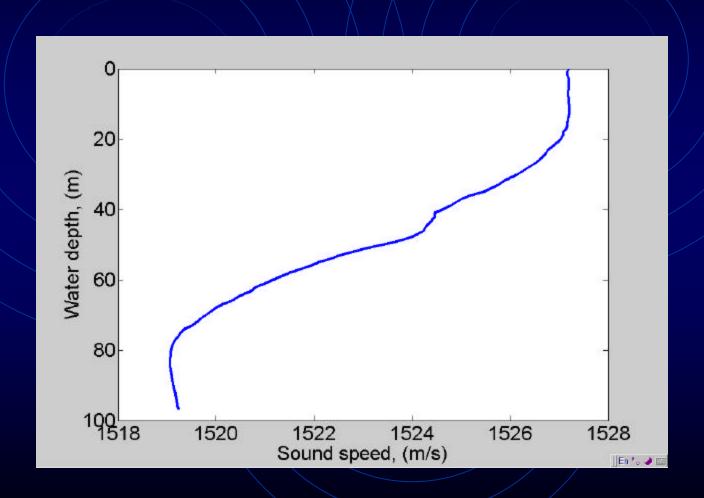
# Model/data comparison procession (mathematically)

Have several different expressions of bottom scattering coefficient

Put those expressions into Reverberation model to get numerical results

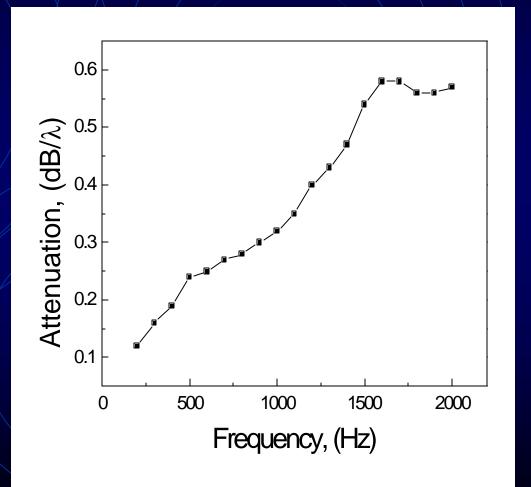
Compare the numerical results with the experimental data to find out the best expression for this experiment

## Sound Speed Profile



#### Bottom parameters

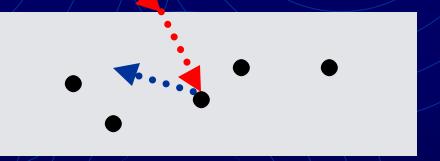
- Bottom speed,1610.8m/s
- Bottom density
   1.86g/cm<sup>3</sup>
- From Geoacoustic
   Inversion by Dr.
   Zhenlin Li





Sediment inhomogeneous

Sediment



- For signal scatterer,  $s \propto k^4$
- Neglect multiple scattering,

$$\mathbf{s}(\mathbf{q}_{i},\mathbf{q}_{s}) = B_{L}k_{2}^{3}|1 + R_{1-2}(\mathbf{q}_{i})|^{2}|1 + R_{1-2}(\mathbf{q}_{s})|^{2} \frac{1}{2\left[\operatorname{Im}\sqrt{\left(\frac{k}{k}\right)^{2} - \cos^{2}\mathbf{q}_{i}} + \operatorname{Im}\sqrt{\left(\frac{k}{k}\right)^{2} - \cos^{2}\mathbf{q}_{s}}\right]}$$

- The above expression approximates to the sediment inhomogeneous model from Jackson, etc.  $W(k) \propto 1/k^0$
- The above expression also approximates perturbation  $|W(k)| \propto 1/k^4$  shness model from Jackson, etc.

#### Published mathematical expressions of bottom scattering coefficient

$$1 s(q_i,q_s) = m \sin(q_i) \sin(q_s)$$

(incomplete)  

$$2 \mathbf{s}(\mathbf{q}_i, \mathbf{q}_s) = \mathbf{m} \sin^{1/2}(\mathbf{q}_i) \sin^{1/2}(\mathbf{q}_s)$$

$$\mathbf{3}_{\mathbf{S}}(\mathbf{q}_{s},\mathbf{q}_{i}) = \mathbf{m} \sin^{l} \left( \frac{\mathbf{q}_{i} + \mathbf{q}_{s}}{2} \right)$$

$$\mathbf{S} = \mathbf{m} \left[ \frac{\sin(\mathbf{q}_i) \sin(\mathbf{q}_s)}{(\sin(\mathbf{q}_i) + \sin(\mathbf{q}_s))} \right]^t$$

$$\mathbf{5} \mathbf{s}(\boldsymbol{q}_{s}, \boldsymbol{q}_{i}) = \mathbf{m} \sin^{l} \left( \cos^{-1} \left( \frac{\cos(\boldsymbol{q}_{i}) + \cos(\boldsymbol{q}_{s})}{2} \right) \right)$$

$$\mathbf{S}(\boldsymbol{q}_{i},\boldsymbol{q}_{s}) \approx \frac{1}{4\boldsymbol{p}} a \left( \frac{\sin(\boldsymbol{q}_{i}) + \sin(\boldsymbol{q}_{s})}{2} k \right)^{2}$$

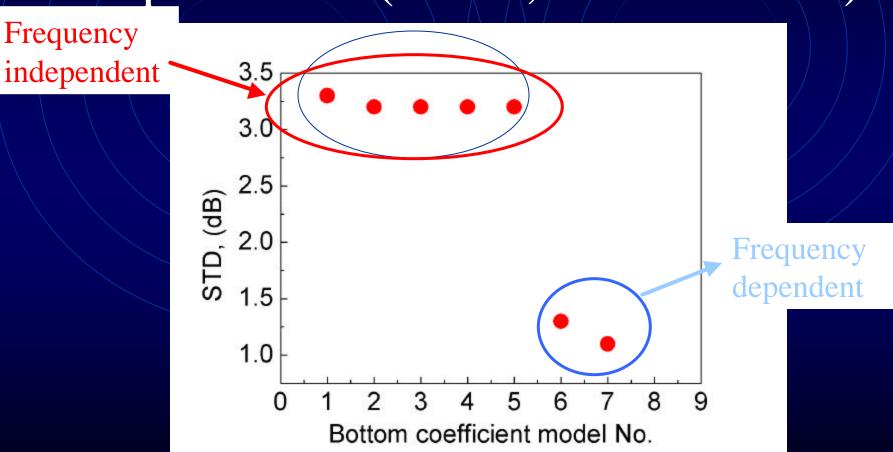
$$\mathbf{s}(\mathbf{q}_{i},\mathbf{q}_{s}) = B_{L}k_{2}^{3}|1 + R_{1-2}(\mathbf{q}_{i})|^{2}|1 + R_{1-2}(\mathbf{q}_{s})|^{2} \frac{1}{2\left[\operatorname{Im}\sqrt{\left(\left(\frac{k}{k}\right)^{2} - \cos^{2}\mathbf{q}_{i}\right) + \operatorname{Im}\sqrt{\left(\left(\frac{k}{k}\right)^{2} - \cos^{2}\mathbf{q}_{s}\right)}\right]}$$

# The criterion for Model/data comparison

Minimum Standard Deviation criterion

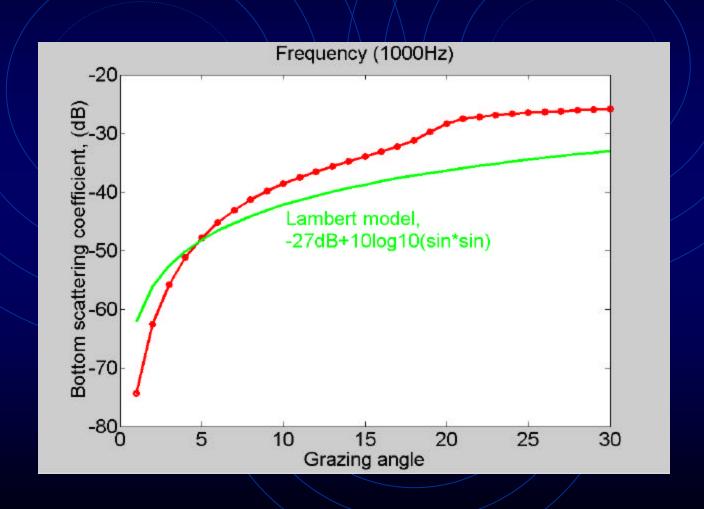
 $\overline{\text{Min(SD)}} = \overline{\text{Min(sqrt(sum(RL_e(t_i)-RL_n(t_i))^2/N))}}$ 

# Standard Derivations for different expressions (2-15s, 700 to 2kHz)

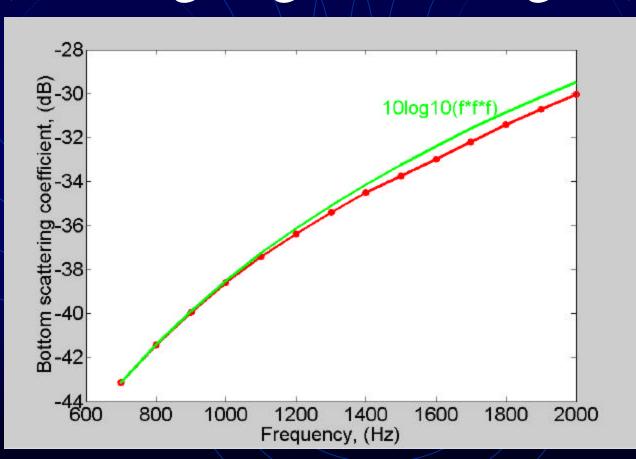


- The bottom scattering coefficient has a strong frequency relationship.
- For explaining 700Hz to 2000Hz experimental RL data, the discrete sediment inhomogeneous model is best model among the models shown in this paper.

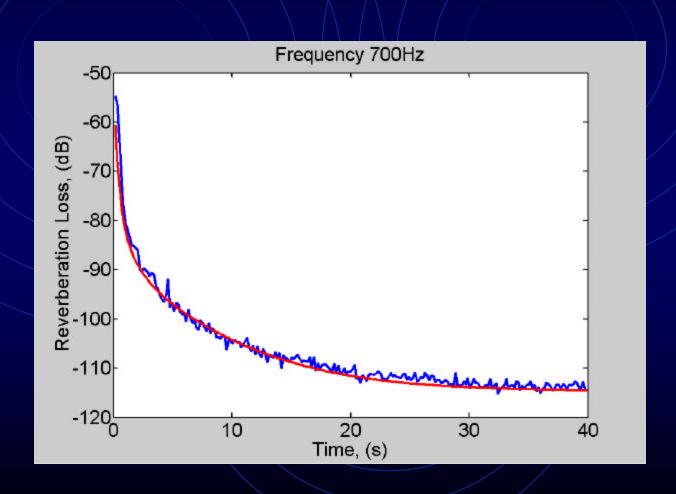
## The bottom scattering coefficient



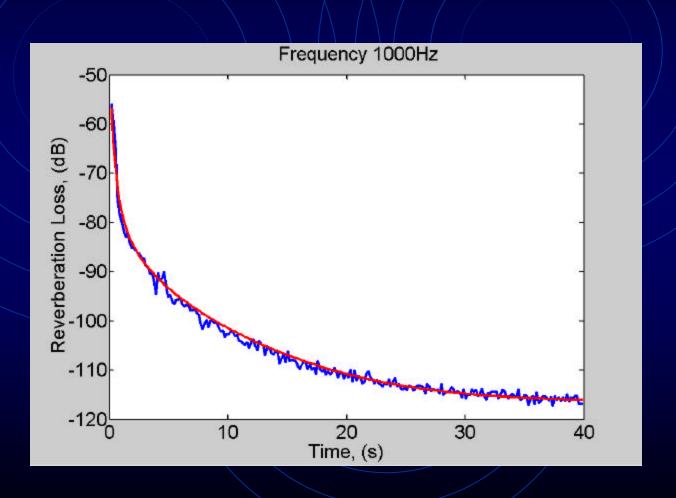
# The bottom scattering coefficient (Grazing angle is 10degree)



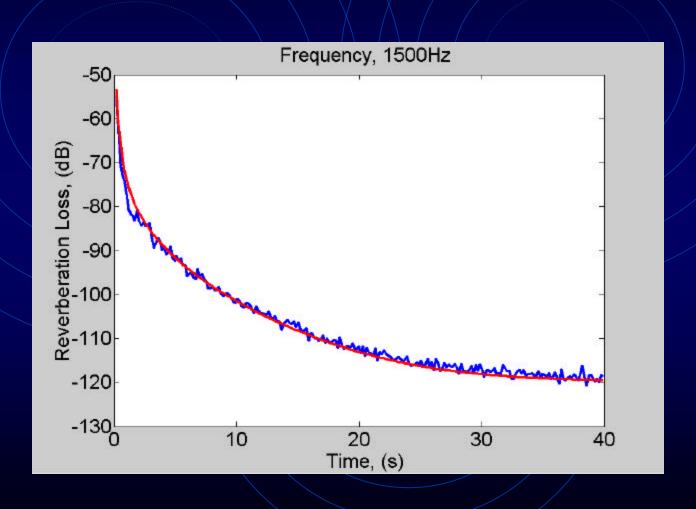
#### Model/data comparison (700Hz)



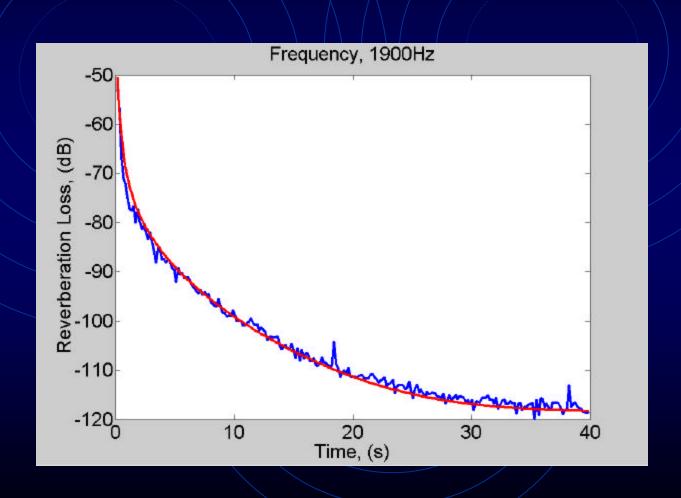
#### Model/data comparison (1000Hz)

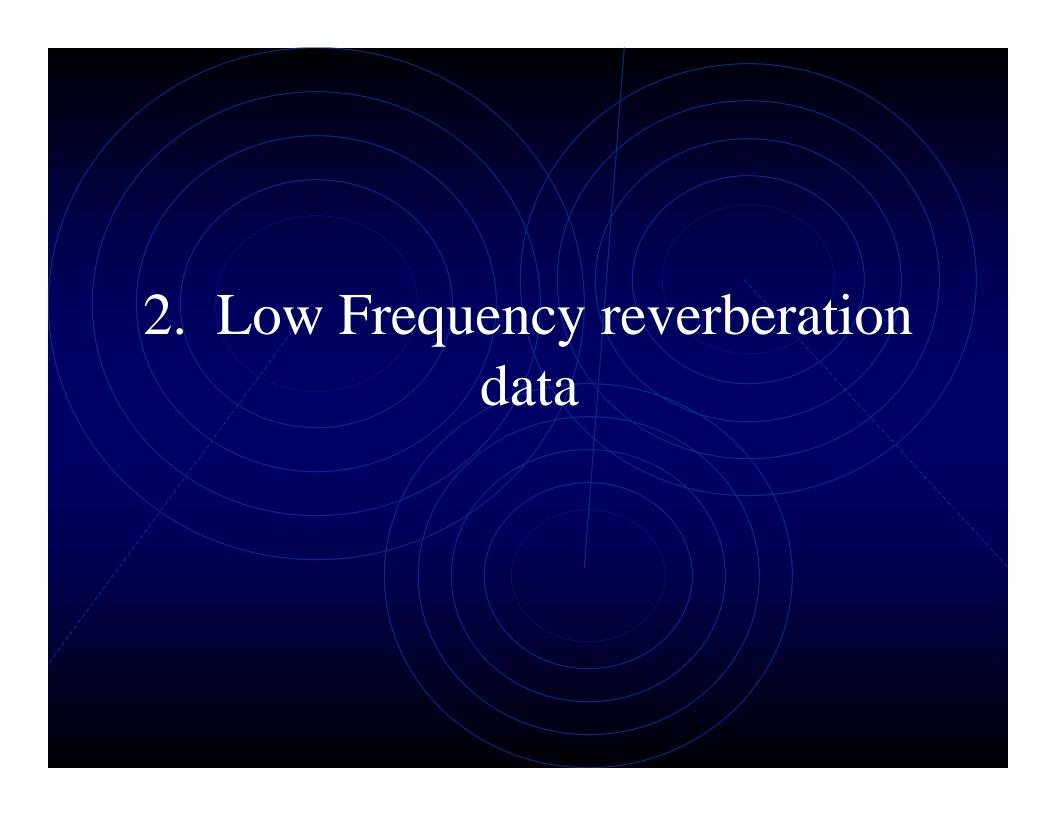


## Model/data comparison (1500Hz)

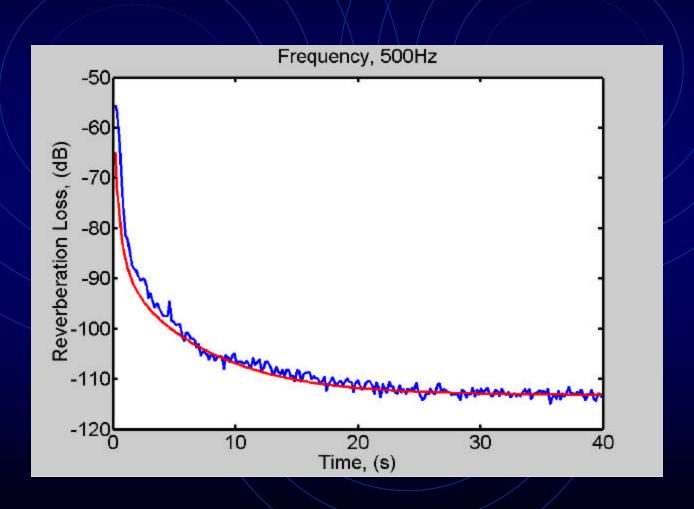


## Model/data comparison (1900Hz)

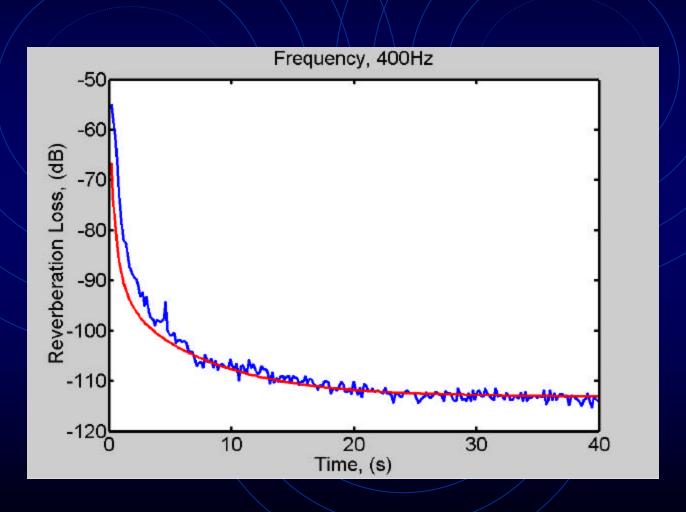




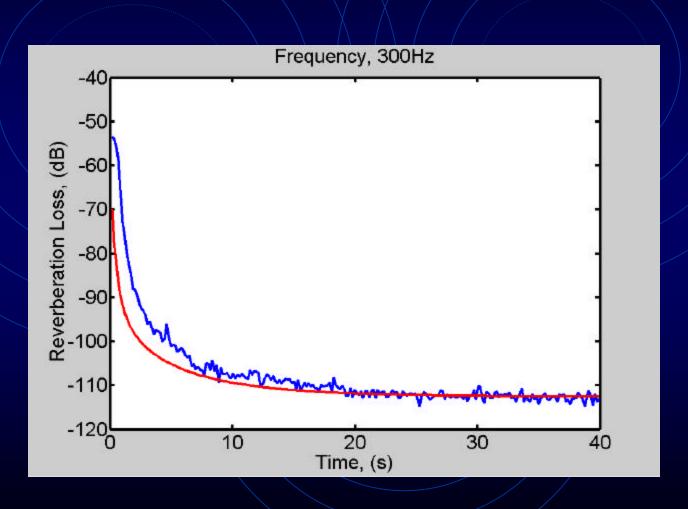
#### Model/data comparison (500Hz)



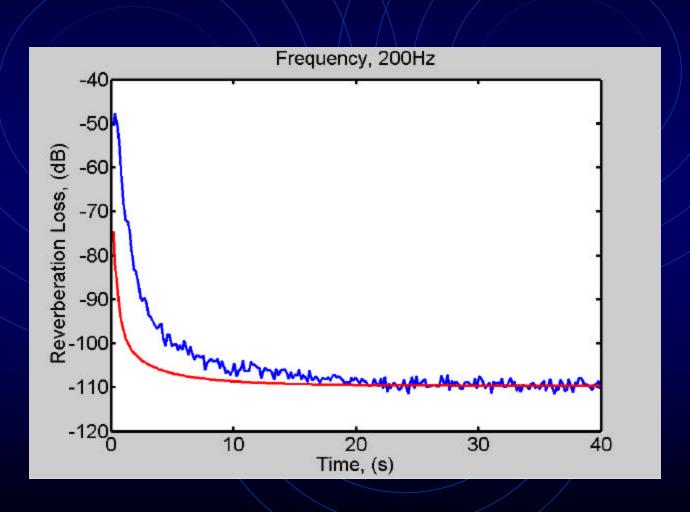
#### Model/data comparison (400Hz)



## Model/data comparison (300Hz)



#### Model/data comparison (200Hz)





Sediment inhomogeneous

Surface roughness

Basement roughness

Sediment

D=15m

Basement

# The sediment-basement combined scattering model

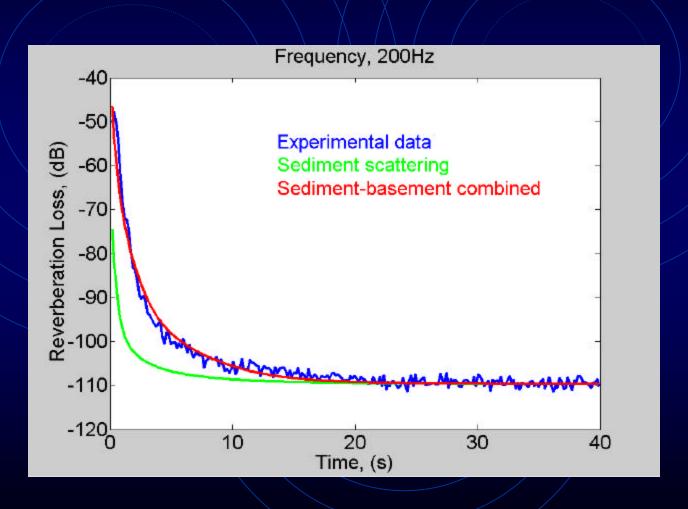
• Bottom scattering includes the scattering from the sediment inhomogeneous and the basement roughness.

$$\mathbf{s}(\mathbf{q}_{i},\mathbf{q}_{s}) = B_{L}k_{2}^{3}|1 + R_{1-2}(\mathbf{q}_{i})|^{2}|1 + R_{1-2}(\mathbf{q}_{s})|^{2} \frac{1}{2\left[\operatorname{Im}\sqrt{\left(\frac{k}{k}\right)^{2} - \cos^{2}\mathbf{q}_{i}}\right] + \operatorname{Im}\sqrt{\left(\frac{k}{k}\right)^{2} - \cos^{2}\mathbf{q}_{s}}\right]} + B_{L}|1 + R_{1-2}(\mathbf{q}_{i})|^{2}|1 + R_{1-2}(\mathbf{q}_{s})|^{2} \exp(-2\mathbf{g}D)W(k)|F(k)|^{2}}$$

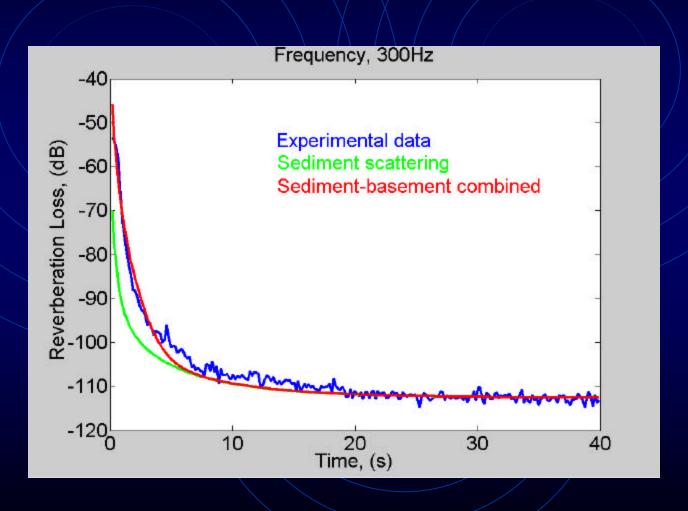
« Ivakin, JASA, 1998, vol. 103»

• D=15m

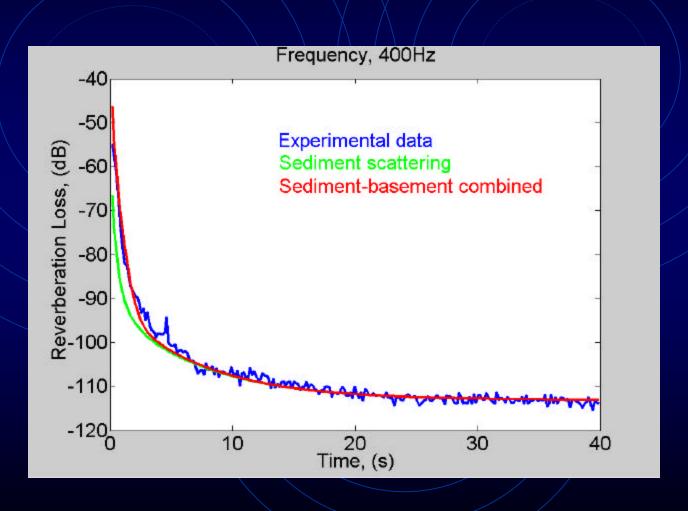
## Model/data comparison (200Hz)



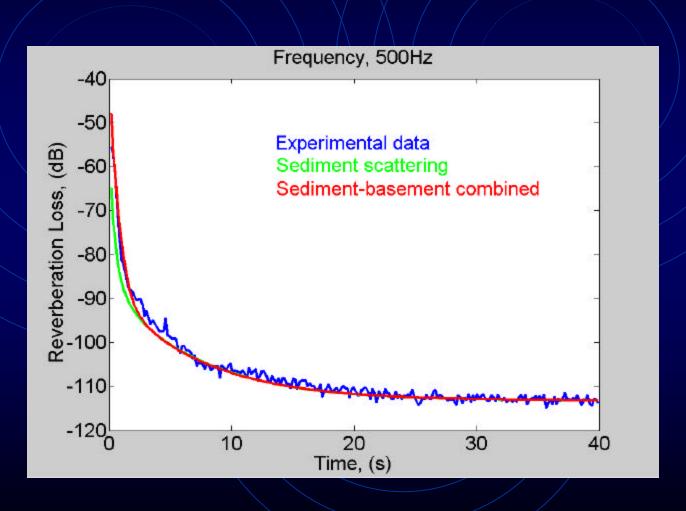
## Model/data comparison (300Hz)



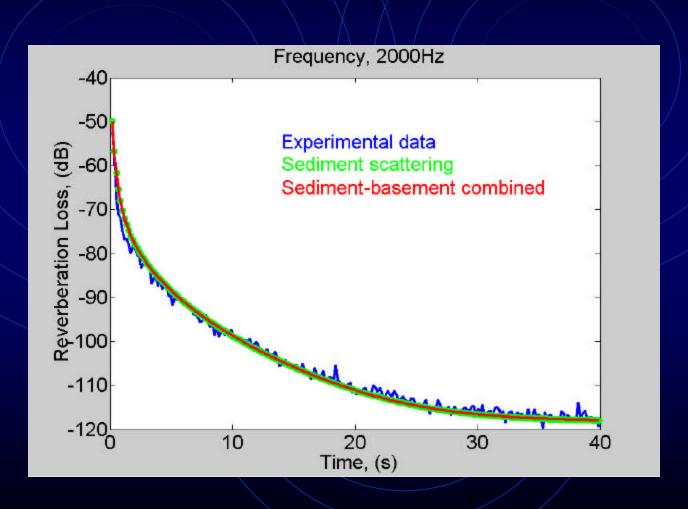
## Model/data comparison (400Hz)



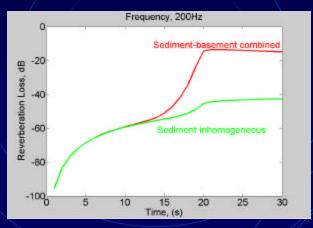
## Model/data comparison (500Hz)

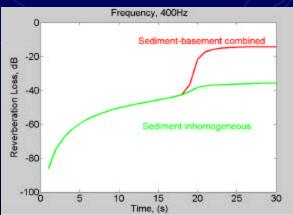


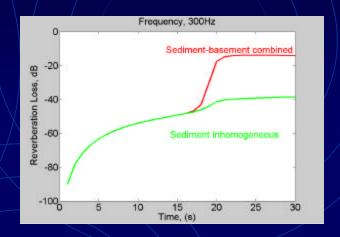
## Model/data comparison (2000Hz)

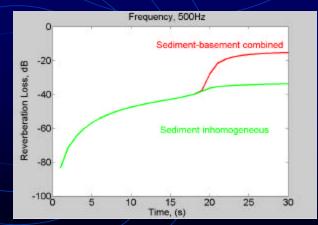


#### Bottom scattering coefficients









#### Summaries

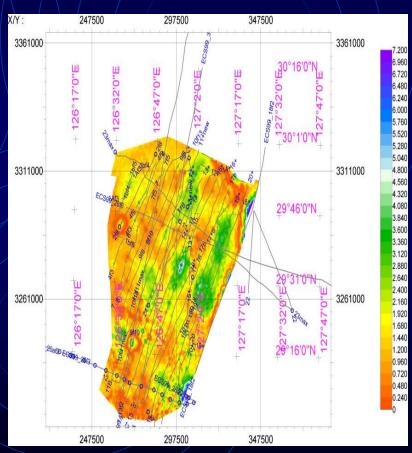
- The bottom scattering coefficient has a strong frequency relationship (f<sup>3</sup>).
- For 700Hz to 2000Hz experimental RL data, the discrete sediment inhomogeneous model is best model among the models shown in this paper.
- The scattering from deeper layer may be a dominating effect for low frequency reverberation data.

#### Other open problems!

- Can this model predict the reverberation correlation?
- How to distinguish the sediment inhomogeneous and surface roughness
- The multiple scattering effect?
- Comparison with the other scattering data?

#### Other open problems!

- Geoacoustic model
  - Basement is not rigid?
  - Sound speed has a positive gradient in the sediment?
  - There is a scattering layer at about 15m?



Seafloor to TST isopach or layer thickness of the top layer of sand-silt in meters. (from L. Bartek)

